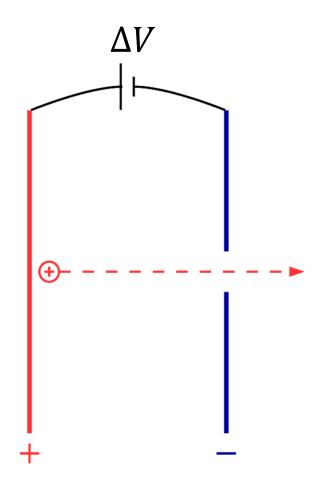
Applications of Electromagnetism (Optional Lecture)

- Particle Accelerators
 - o Linear Accelerators
 - o Cyclotrons
- Beamline Magnets
 - Steering Magnets
 - Focusing Magnets
- Velocity Selectors
- Detectors
 - Spectrometers
 - o Drift Chambers

Linear Accelerator

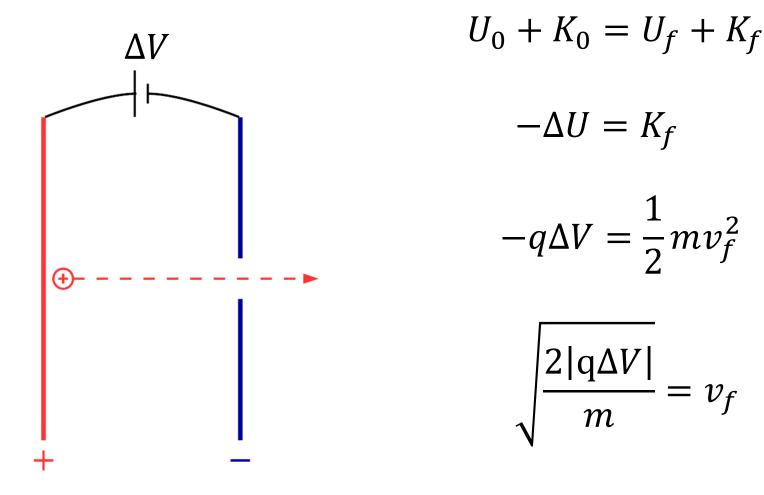
Charged particles are accelerated across a potential difference.



$$\vec{F} = q\vec{E}$$

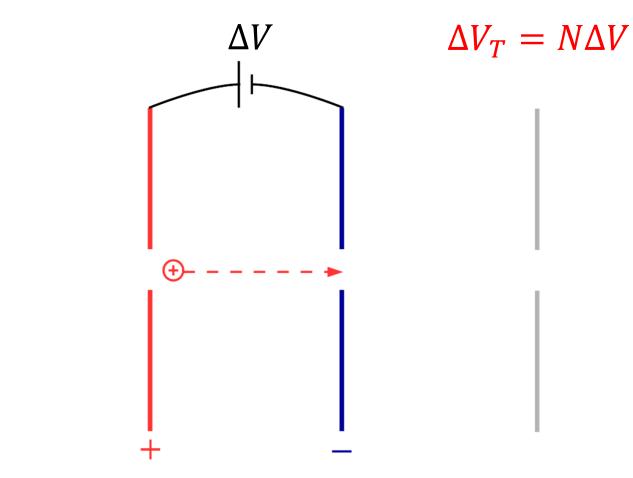
Linear Accelerator

Charged particles are accelerated across a potential difference.

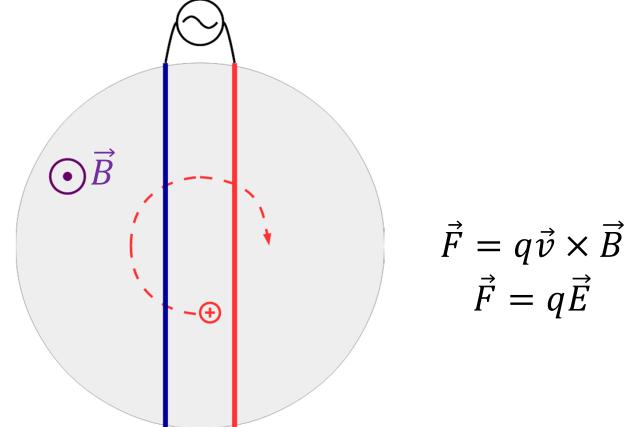


Linear Accelerator

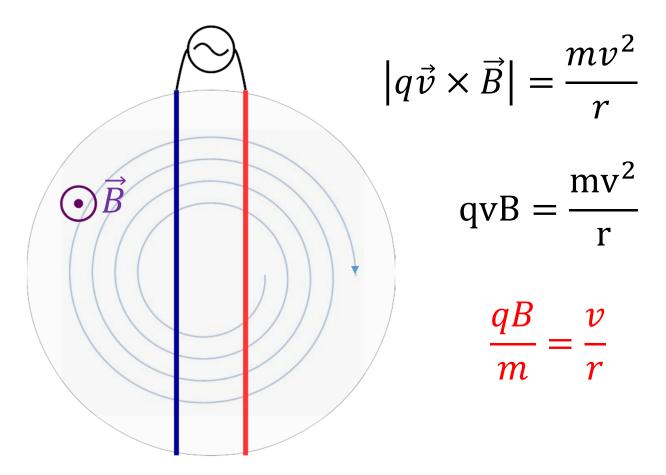
Potential difference across plates when particle is between plates. (*N* regions between plates)



If you want to accelerate particles and are limited on space - keep sending them through the same two plates.



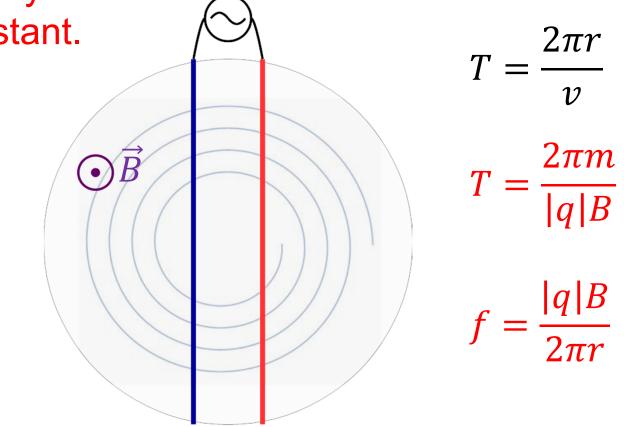
Particles spiral out as they accelerate, increasing speed and radius proportionally.



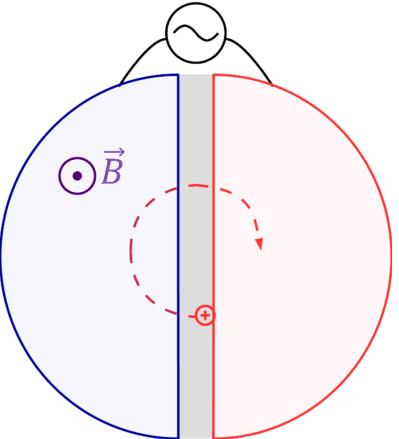
Particles spiral out as they accelerate, increasing speed and radius proportionally so that the period and frequency

remain constant.

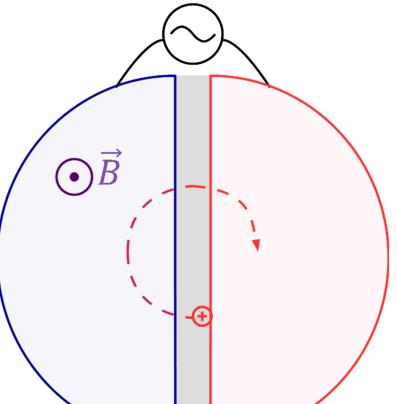
$$\frac{|q|B}{m} = \frac{v}{r}$$



Instead of plates, use "D's", hollow D-shaped conductors with a top, a bottom and an outside edge.



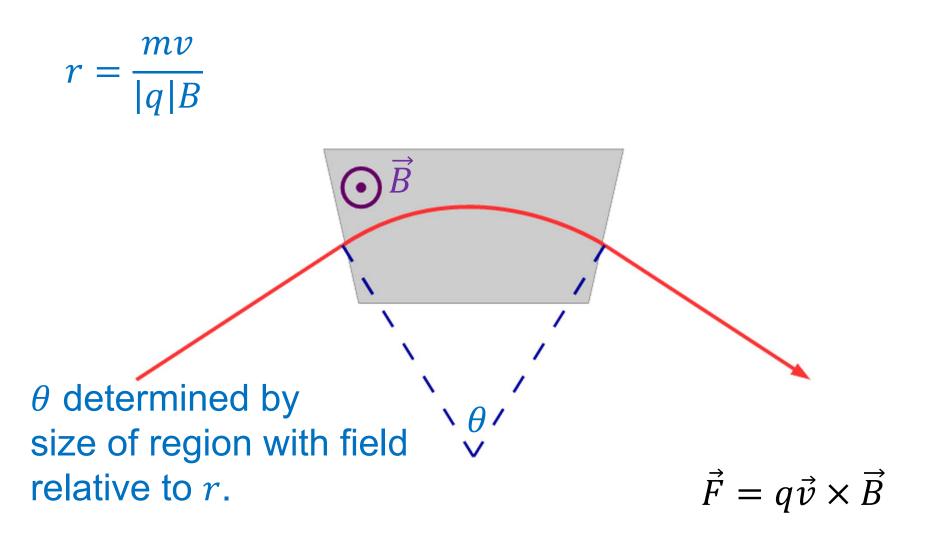
Instead of plates, use "D's", hollow *D*-shaped conductors with a top, a bottom and an outside edge.



Modern cyclotrons use complex electromagnetic fields created without D's.

Steering Magnets

Beamlines are turned with steering magnets.



Focusing Magnets

Beamlines are focused with special magnets.



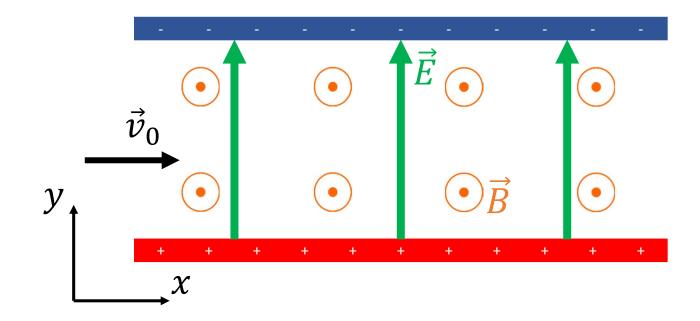
$\vec{F} = q\vec{v} \times \vec{B}$

(Unfortunately, a magnet can only focus in one transverse dimension and at one location along the beam. Beamlines may have many such focusing magnets.)

Velocity Selector (See previous lecture.)

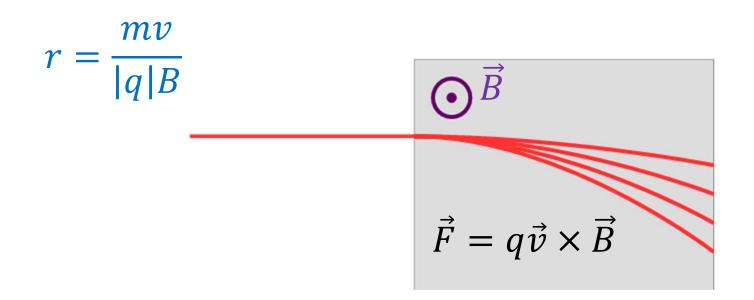
If $v_0 = \frac{E}{B}$, then $\vec{F} = 0$ and the trajectory is a straight line.

 $\vec{F} = q\left(\vec{E} + \vec{v} \times \vec{B}\right)$



Spectrometers

Consider a bending magnet with a back wall that registers interactions with charged particles. The particles will separate according to their radius of curvature.



Spectrometers

Consider nuclei that have been accelerated across a potential difference ΔV yielding a radius of curvature in the magnetic field

$$r = \frac{1}{B} \sqrt{\frac{2m\Delta V}{q}} \sim \sqrt{\frac{m}{q}} \sim \sqrt{\frac{A}{Z}}$$

Spectrometers

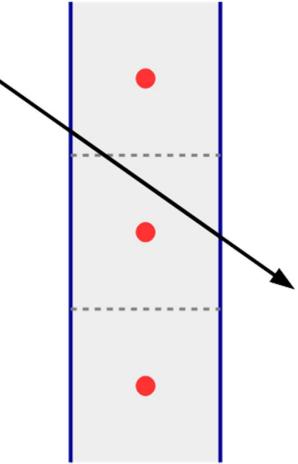
Isotope	$\sqrt{A/Z}$	
¹³ ₇ N	$\sqrt{13/7}$	
$^{14}_{7}N$	$\sqrt{2}$	
¹⁵ ₇ N	$\sqrt{15/7}$	
¹⁶ ₈ 0	$\sqrt{2}$	0
¹⁷ ₈ 0	$\sqrt{17/8}$	
¹⁸ ₈ 0	$\sqrt{9/4}$	

Separation of fully ionized isotopes by mass to charge ratio.

$$r = \frac{1}{B} \sqrt{\frac{2m\Delta V}{q}} \sim \sqrt{\frac{m}{q}} \sim \sqrt{\frac{A}{Z}}$$

Drift Chambers

Drift chambers signal the passage of ionizing particles.

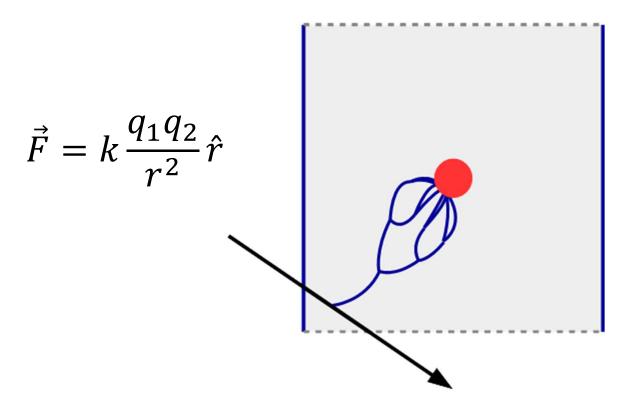


Drift Chambers

- Passing particle ionizes atoms in gas.
- Free electrons accelerate towards cathode.
- Electrons ionize more atoms on way to cathode.

 $\vec{F} = q\vec{E}$

• Momentary measureable current created.



Accelerator Physics

Examples from today's lecture:

- Particles accelerated with electric fields.
- Particle beams steered with magnetic fields.
- Particle beams focused with magnetic fields.
- Particle velocities selected with crossed electric and magnetic fields.
- Particles identified with magnetic fields.
- Particle location and direction determined with electric fields.