PHYS 2135 Exam III

April 23, 2019

Name: Section:

For questions 1-5, select the best answer. For problems 6-10, solutions must begin with an Official Starting Equation, when appropriate. Work must be shown to receive credit. Calculators are not allowed.

(8) **B 1.** Two long, straight, parallel wires carry identical currents in opposite directions. The force between the two wires is

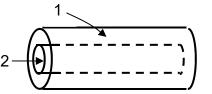
[A]	attractive	[B]	repulsive
[C]	zero	[D]	indeterminate

 (8) C 2. Two solenoids, wound in the same direction, are coaxial as shown. Solenoid 1, outer, has 1000 turns/meter and twice the radius of solenoid 2, inner, which has 2000 turns/meter. What direction and ratio of currents, *l*₁/*l*₂ will result in zero magnetic field near the axis of solenoid 2?
 [A] *l*₁/*l*₂=2, currents in same direction

[B] $I_1/I_2=1/2$, currents in same direction

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- [C] $l_1/l_2=2$, currents in opposite direction
- [D] $I_1/I_2=1/2$, currents in opposite direction

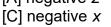


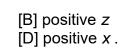
- (8) **B 3.** A circular conducting loop is pushed into a region of uniform magnetic field, directed into the page as shown in the diagram. In which direction will the induced current flow?



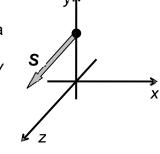
(8) **D 4.** The figure to the right shows the direction of propagation (Poynting vector) of an electromagnetic wave at a certain point in space and a certain instant in time. If the magnetic field direction at this point and time is in the positive *y* direction, what is the direction of the electric field at this point

and time? [A] negative *z*





[D]



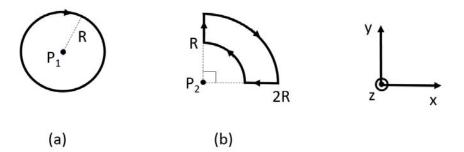
(8) **5** (Free). Electric and magnetic fields

[A] are hard to plow.

- [B] provide a good foundation for power lines.
- [C] flourish in sunlight.
- [D] need water to grow currants.



6. Two thin wires are shaped as in the figure (a) and (b) below. They each carry a steady current I in the direction indicated by the arrows.



(15) (a) Calculate the magnitude and direction of the magnetic field at the center P_1 of the loop of radius R as a function of μ_0 , I, and R. You must show the steps of your derivation and explain the result to get credit.

$$d\vec{B} = \frac{\mu_0 I}{4\pi} \frac{d\vec{s} \times \hat{r}}{r^2}$$
$$\vec{B} = \frac{\mu_0 I}{4\pi} \int_0^{2\pi} \frac{R d\phi(-\hat{\phi}) \times (-\hat{r})}{R^2}$$
$$\vec{B} = \frac{\mu_0 I}{4\pi R} \int_0^{2\pi} d\phi (-\hat{k})$$
$$\vec{B} = \frac{-2\pi\mu_0 I}{4\pi R} \hat{k}$$
$$\vec{B} = -\frac{\mu_0 I}{2R} \hat{k}$$

(25) (b) Calculate the magnitude and direction of the magnetic field at the point P₂ as a function of μ_0 , I, and R. You must show the steps of your derivation and explain the result to get credit. The inner arc has a radius R and the outer arc has a radius 2R.

For the two straight segments, $d\vec{s} \parallel \hat{r}$. Thus, they do not contribute to \vec{B} .

For the inner arc:

$$\vec{B}_{I} = \frac{\mu_{0}I}{4\pi} \int_{0}^{\pi/2} \frac{Rd\phi \hat{\phi} \times (-\hat{r})}{R^{2}} \qquad \vec{B}_{O} = \frac{\mu_{0}I}{4\pi} \int_{0}^{\pi/2} \frac{2Rd\phi(-\hat{\phi}) \times (-\hat{r})}{(2R)^{2}}$$

$$\vec{B}_{I} = \frac{\mu_{0}I}{4\pi R} \left(\frac{\pi}{2}\right) \hat{k} \qquad \vec{B}_{O} = \frac{-\mu_{0}I}{8\pi R} \left(\frac{\pi}{2}\right) \hat{k}$$

$$\vec{B} = \left(\frac{\mu_{0}I}{8R} - \frac{\mu_{0}I}{16R}\right) \hat{k}$$

$$\vec{B} = \frac{\mu_{0}I}{16R} \hat{k}$$
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7. Consider an ideal toroidal solenoid with *N* turns, each carrying a current *I* directed as shown in the figure. Applying Ampere's law, find the direction and magnitude of the magnetic field in the following regions:

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\rm enc}$$

There is no enclosed current. $\vec{B} = 0$.

* * * * * N turns

current I2, mass M

length, L

out of page (\odot)

wire '①'

wire '2

d

 $B(2\pi r) = \mu_0 NI$ $B = \frac{\mu_0 NI}{2\pi r}$ Counter-Clockwise (By the right hand rule)

(into page (⊗

8. As shown in the figure, a long straight wire, labeled

(1), carries a current *I*₁ and is fixed in position. Wire
(2), of length *L* and mass *M*, carries a current *I*₂ and is placed a distance *d* from wire (1).

 $\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\rm enc}$

(10) (a) Applying Ampere's law, find the direction and magnitude of the magnetic field produced at wire (2) by wire (1).

Direction: (circle one) up (\uparrow) down (\downarrow)

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{enc}$$
$$B(2\pi d) = \mu_0 I_1$$
$$B = \frac{\mu_0 I_1}{2\pi d}$$

(10) (b) Wire (2) does not fall, but stays at the same vertical position. Under this condition, find the direction of the current in wire (2). Also, express the distance *d* in terms of I_1 , I_2 , *L*, *M*, and constants. Note that gravity is NOT ignorable.

Direction: (circle one)

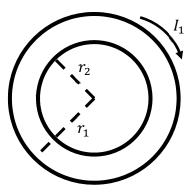
$$F_{g} = F_{B}$$

$$Mg = |I_{2}\vec{L}_{2} \times \vec{B}_{1}| = I_{2}L\left(\frac{\mu_{0}I_{1}}{2\pi d}\right)$$

$$d = \frac{\mu_{0}I_{1}I_{2}L}{2\pi Mg}$$
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- **9.** The current in a long solenoid is given by $I_1 = I_0 e^{-\alpha t}$ and is clockwise as illustrated in the figure. The solenoid has N_1 windings, length L_1 , radius r_1 and resistance R_1 . A single circular wire loop of radius $r_2 < r_1$ and resistance R_2 is placed at the center of the solenoid as shown in the figures. (I_0 and α are both positive quantities.
- (10) (a) In what direction is the induced current in the loop for t > 0? [Circle the correct answer.] [A] Clockwise [B] Counter-clockwise





(20) (b) Determine the induced emf
$$\mathcal{E}$$
 in the loop for $t > 0$

$$B_{1} = \mu_{0} n_{1} I_{1}$$

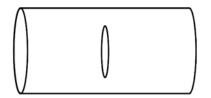
$$B_{1} = \mu_{0} \left(\frac{N_{1}}{L_{1}}\right) I_{0} e^{-\alpha t}$$

$$\mathcal{E} = -\frac{d}{dt} \phi_{B}$$

$$\mathcal{E} = -\frac{d}{dt} \left[\mu_{0} \left(\frac{N_{1}}{L_{1}}\right) I_{0} e^{-\alpha t} (\pi r_{2}^{2})\right]$$

$$\mathcal{E} = \frac{\mu_{0} N_{1} I_{0} \alpha \pi r_{2}^{2}}{L_{1}} e^{-\alpha t}$$





(10) (c) Determine the current I_2 in the loop for t > 0.

$$I_2 = \frac{\varepsilon}{R_2}$$
$$I_2 = \frac{\mu_0 N_1 I_0 \alpha \pi r_2^2}{L_1 R_2} e^{-\alpha t}$$

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- **10.** A satellite located a distance H above the surface of the earth emits a radio signal of frequency f uniformly in all directions. The signal with intensity I₀ is received by a totally absorbing square antenna with side length L on the surface of the earth that is perpendicular to the incoming signal. All answers should be expressed in terms of H, f, I₀, L, and fundamental constants.
- (10) (a) What is the power of the signal generated by the satellite?

$$I = \frac{P}{A}$$
$$P = 4\pi H^2 I_0$$

(10) (b) What is the maximum electric field at the location of the antenna?

$$I = c \langle u \rangle = c \left(\frac{1}{2} \epsilon_0 E_{\max}^2 \right)$$
$$\sqrt{\frac{2I_0}{c\epsilon_0}} = E_{\max}$$

(10) (c) What is the average energy density delivered to the antenna by the electric field?

$$\langle u_E \rangle = \frac{1}{2} \langle u \rangle = \frac{1}{2} \left(\frac{I_0}{c} \right)$$

(10) (d) What force does the radiation exert on the antenna?

$$\frac{F}{A} = \langle P_{\text{rad}} \rangle = \frac{I}{c}$$
$$F = \frac{I_0 L^2}{c}$$

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