

Official Starting Equations
PHYS 2135, Engineering Physics II

From PHYS 1135:

$$x = x_0 + v_{0x}\Delta t + \frac{1}{2}a_x(\Delta t)^2 \quad v_x = v_{0x} + a_x\Delta t \quad v_x^2 = v_{0x}^2 + 2a_x(x - x_0) \quad \sum \vec{F} = m\vec{a}$$

$$F_r = -\frac{mv_t^2}{r} \quad P = \frac{F}{A} \quad \vec{p} = m\vec{v} \quad P = \frac{dW}{dt} \quad W = \int \vec{F} \cdot d\vec{s}$$

$$K = \frac{1}{2}mv^2 \quad U_f - U_i = -W_{\text{conservative}} \quad E = K + U \quad E_f - E_i = (W_{\text{other}})_{i \rightarrow f} \quad E = P_{\text{ave}}t$$

Constants:

$$g = 9.8 \frac{\text{m}}{\text{s}^2} \quad m_{\text{electron}} = 9.11 \times 10^{-31} \text{kg} \quad m_{\text{proton}} = 1.67 \times 10^{-27} \text{kg} \quad e = 1.6 \times 10^{-19} \text{C}$$

$$c = 3.0 \times 10^8 \frac{\text{m}}{\text{s}} \quad k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} \quad \epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2} \quad \mu_0 = 4\pi \times 10^{-7} \frac{\text{Tm}}{\text{A}}$$

Electric Force, Field, Potential and Potential Energy:

$$\vec{F} = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12} \quad \vec{E} = k \frac{q}{r^2} \hat{r} \quad \vec{F} = q\vec{E} \quad \Delta V = -\int_i^f \vec{E} \cdot d\vec{s}$$

$$U = k \frac{q_1 q_2}{r_{12}} \quad V = k \frac{q}{r} \quad \Delta U = q\Delta V \quad E_x = -\frac{\partial V}{\partial x}$$

$$\vec{p} = q\vec{d} \text{ (from - to +)} \quad \vec{\tau} = \vec{p} \times \vec{E} \quad U_{\text{dipole}} = -\vec{p} \cdot \vec{E}$$

$$\Phi_E = \int_S \vec{E} \cdot d\vec{A} \quad \oint_S \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_0} \quad \lambda \equiv \frac{\text{charge}}{\text{length}} \quad \sigma \equiv \frac{\text{charge}}{\text{area}} \quad \rho \equiv \frac{\text{charge}}{\text{volume}}$$

Circuits:

$$C = \frac{Q}{V} \quad \frac{1}{C_T} = \sum \frac{1}{C_i} \quad C_T = \sum C_i \quad C_0 = \frac{\epsilon_0 A}{d} \quad C = \kappa C_0$$

$$U = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C} = \frac{1}{2}QV \quad I = \frac{dq}{dt} \quad J = \frac{I}{A} \quad \vec{J} = nq\vec{v}_d$$

$$\vec{J} = \sigma\vec{E} \quad V = IR \quad R = \rho \frac{L}{A} \quad \sigma = \frac{1}{\rho} \quad \rho = \rho_0[1 + \alpha(T - T_0)]$$

$$\sum I = 0 \quad \sum \Delta V = 0 \quad \frac{1}{R_T} = \sum \frac{1}{R_i} \quad R_T = \sum R_i \quad P = IV = \frac{V^2}{R} = I^2 R$$

$$Q(t) = Q_{\text{final}}[1 - e^{-t/\tau}] \quad Q(t) = Q_0 e^{-t/\tau} \quad \tau = RC$$

Integral:

$$\int \frac{du}{(u^2+a^2)^{3/2}} = \frac{u}{a^2\sqrt{u^2+a^2}} + c$$

Magnetic Force, Field and Inductance:

$$\begin{aligned}\vec{F} &= q(\vec{E} + \vec{v} \times \vec{B}) & \vec{F} &= I\vec{L} \times \vec{B} & \Phi_B &= \int \vec{B} \cdot d\vec{A} & \oint \vec{B} \cdot d\vec{A} &= 0 \\ \oint \vec{B} \cdot d\vec{s} &= \mu_0 I_{\text{enclosed}} & \vec{\mu} &= NI\vec{A} & \vec{\tau} &= \vec{\mu} \times \vec{B} & U_{\text{dipole}} &= -\vec{\mu} \cdot \vec{B} \\ \vec{B} &= \frac{\mu_0 q \vec{v} \times \hat{r}}{4\pi r^2} & d\vec{B} &= \frac{\mu_0 I d\vec{s} \times \hat{r}}{4\pi r^2} & \mathcal{E} &= -N \frac{d\Phi_B}{dt} & \oint \vec{E} \cdot d\vec{s} &= -\frac{d\Phi_B}{dt} \\ \oint \vec{B} \cdot d\vec{s} &= \mu_0 I_{\text{enclosed}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} & B &= \frac{\mu_0 I}{2\pi r} & B &= \mu_0 nI\end{aligned}$$

Electromagnetic Waves:

$$\begin{aligned}I &= \frac{P}{A} & u &= \frac{1}{2}(\epsilon_0 E^2 + \frac{B^2}{\mu_0}) = \epsilon_0 E^2 = \frac{B^2}{\mu_0} & \langle u \rangle &= \frac{1}{4}(\epsilon_0 E_{\text{max}}^2 + \frac{B_{\text{max}}^2}{\mu_0}) = \frac{1}{2}\epsilon_0 E_{\text{max}}^2 = \frac{B_{\text{max}}^2}{2\mu_0} \\ \frac{E}{B} &= c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} & \vec{S} &= \frac{1}{\mu_0} \vec{E} \times \vec{B} & I &= \langle S \rangle = c \langle u \rangle & \langle P_{\text{rad}} \rangle &= \frac{I}{c} \text{ or } \frac{2I}{c} \\ k &= \frac{2\pi}{\lambda} & \omega &= 2\pi f & T &= \frac{1}{f} & v &= f\lambda = \frac{\omega}{k} = \frac{c}{n}\end{aligned}$$

Optics:

$$\begin{aligned}I &= I_{\text{max}} \cos^2 \phi & \theta_r &= \theta_i & n &= \frac{c}{v} = \frac{\lambda_0}{\lambda_n} & n_r \sin \theta_r &= n_i \sin \theta_i \\ \frac{1}{s} + \frac{1}{s'} &= \frac{1}{f} & m &= \frac{y'}{y} = -\frac{s'}{s} & \frac{1}{f} &= (n-1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right) & f &= \frac{R}{2} \\ \frac{n_a}{s} + \frac{n_b}{s'} &= \frac{n_b - n_a}{R} & m &= \frac{y'}{y} = -\frac{n_a s'}{n_b s} & \Delta L &= m\lambda & \Delta L &= \left(m + \frac{1}{2}\right)\lambda \\ \Delta L &= d \sin \theta & \phi &= 2\pi \left(\frac{\Delta L}{\lambda}\right) & I &= I_0 \cos^2 \frac{\phi}{2} & R &= \frac{\lambda}{\Delta \lambda} = Nm \\ m\lambda &= a \sin \theta & \beta &= \frac{2\pi}{\lambda} a \sin \theta & I &= I_0 \left[\frac{\sin(\beta/2)}{\beta/2} \right]^2\end{aligned}$$

Integral:

$$\int \frac{du}{(u^2 + a^2)^{3/2}} = \frac{u}{a^2 \sqrt{u^2 + a^2}} + c$$

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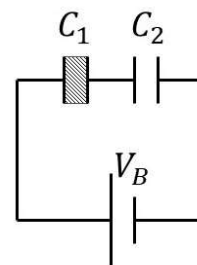
PHYS 2135 Exam II
October 25, 2022

Name: _____ Section: _____

For questions 1-5, select the best answer. For problems 6-11, solutions must begin with an Official Starting Equation, when appropriate. Work must be shown to receive credit. Calculators are not allowed. Use appropriate units. Provide answers in terms of given variable and fundamental constants.

- (8) _____ **1.** A constant electric field is maintained inside a piece of copper while increasing its temperature. What happens to the current density inside the copper?
- [A] increases
 - [B] decreases
 - [C] remains unchanged
 - [D] not enough information
- (8) _____ **2.** A Duracell 9V battery is connected to an external 100 kilo-ohm resistor. If the external resistor is now changed to a 10 ohm resistor, how will the battery's terminal voltage change?
- [A] increase
 - [B] decrease
 - [C] remains unchanged
 - [D] not enough information
- (8) _____ **3.** A simple circuit consists of a 12 V power supply and two one kilo-ohm resistors in series. To measure the voltage across one of the resistors, a student hooks up his voltmeter in series. What will happen?
- [A] A large current will flow; smoke, fire, tears, and a broken meter
 - [B] Very little current will flow. The meter will display approximately 12 V.
 - [C] The meter will correctly measure 6 V.
 - [D] The meter's readings will jump all over the place
- (8) _____ **4.** A charged particle with non-zero velocity is moving within a uniform magnetic field. The particle's velocity vector is perpendicular to the magnetic field. Describe the particle's motion.
- [A] The particle moves in a circle
 - [B] The particle moves in a helix.
 - [C] The particle drifts in a straight line at constant velocity.
 - [D] The particle will move in an ellipse
- (8) _____ **5.** (Free) If a 300 V power supply is hooked up to an electrolytic capacitor rated for 10 V, what will happen?
- [A] It contacts HR and presses charges
 - [B] It explodes and reincarnates as a supercapacitor
 - [C] Its magic smoke is captured, distilled, and vaped by EE students
 - [D] It's unfortunate, but life isn't farad all

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6. A pair of identical parallel plate capacitors with capacitance C_0 are connected in series to a battery with potential difference V_B . The gap of the first capacitor C_1 is filled with a dielectric of dielectric constant κ as illustrated. [Answers should be given in terms of C_0 , V_B and κ .]

(15) a. Determine C_T the total capacitance of the pair of capacitors after the dielectric has been added.

$C_T =$

(10) b. Determine Q_1 the charge on C_1 long after the dielectric has been added.

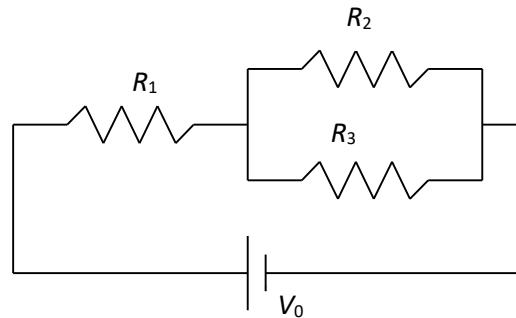
$Q_1 =$

(15) c. Determine U_1 the energy stored on C_1 long after the dielectric has been added.

$U_1 =$

7. For the resistor system shown, $R_1 = R_0$, $R_2 = 3R_0$, and $R_3 = 6R_0$. Find ...

(15) a. R_T the equivalent resistance, and



$R_T =$

(15) b. the current through each resistor.

$I_1 =$

$I_2 =$

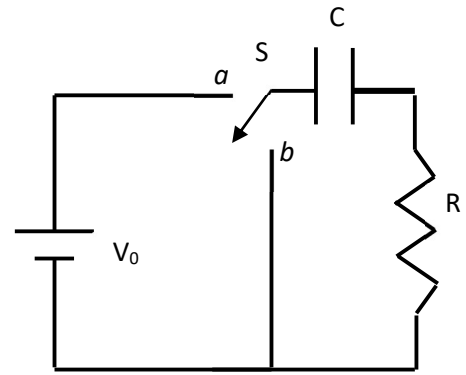
$I_3 =$

(10) c. Assume that $R_0 = 100 \Omega$. If the maximum power that can safely be delivered to R_2 is 3 W, what is the maximum voltage that can be applied to the circuit?

$V_{0\text{-max}} =$

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8. In the circuit shown there is an uncharged capacitor C , a resistor R , and a switch S . They are in series with a battery of voltage V_0 .



(10) a. The switch S is set to 'a' to charge the capacitor. After a long time, what will be the charge on the capacitor?

$$Q_f =$$

(10) b. What is the final energy stored in the capacitor?

$$U_f =$$

(10) c. How long does it take for the stored energy in the capacitor to be reduced to one-quarter ($1/4$) of its original value?

$$t =$$

(10) d. What is the voltage across the resistor when the stored energy is $1/4$ th of its original value?

$$V_R =$$

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9. A proton moves perpendicularly to a uniform magnetic field \mathbf{B} at a speed $v = 1.67 \times 10^7$ m/s and experiences an acceleration $a = 3.2 \times 10^{13}$ m/s² in the positive x -direction when its velocity is in the positive z -direction.

(8) a. What is the magnitude of the magnetic field B ?

(8) b. What is the direction of the magnetic field?

10. A long, straight wire carries a current $I = 15$ A directed along the positive x -axis and perpendicular to a magnetic field. The wire experiences a magnetic force per unit length of 0.30 N/m in the negative y -direction.

(8) a. What is the magnitude of the magnetic field?

(8) b. What is the direction of the magnetic field?

11. A current $I = 10.0$ mA is maintained in a single circular loop with a radius $r = 20.0$ cm. A magnetic field of magnitude $B = 0.50$ T is directed in the plane of the loop.

(8) What is the magnitude of the torque exerted by the magnetic field on the loop? [Express your numerical result in terms of π or use $\pi = 3.14$]