

**Official Starting Equations**  
**PHYS 2135, Engineering Physics II**

**From PHYS 1135:**

$$x = x_0 + v_{0x}\Delta t + \frac{1}{2}a_x(\Delta t)^2 \quad v_x = v_{0x} + a_x\Delta t \quad v_x^2 = v_{0x}^2 + 2a_x(x - x_0) \quad \sum \vec{F} = m\vec{a}$$

$$F_r = -\frac{mv_t^2}{r} \quad P = \frac{F}{A} \quad \vec{p} = m\vec{v} \quad P = \frac{dW}{dt} \quad W = \int \vec{F} \cdot d\vec{s}$$

$$K = \frac{1}{2}mv^2 \quad U_f - U_i = -W_{\text{conservative}} \quad E = K + U \quad E_f - E_i = (W_{\text{other}})_{i \rightarrow f} \quad E = P_{\text{ave}}t$$

**Constants:**

$$g = 9.8 \frac{\text{m}}{\text{s}^2} \quad m_{\text{electron}} = 9.11 \times 10^{-31} \text{kg} \quad m_{\text{proton}} = 1.67 \times 10^{-27} \text{kg} \quad e = 1.6 \times 10^{-19} \text{C}$$

$$c = 3.0 \times 10^8 \frac{\text{m}}{\text{s}} \quad k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} \quad \epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2} \quad \mu_0 = 4\pi \times 10^{-7} \frac{\text{Tm}}{\text{A}}$$

**Electric Force, Field, Potential and Potential Energy:**

$$\vec{F} = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12} \quad \vec{E} = k \frac{q}{r^2} \hat{r} \quad \vec{F} = q\vec{E} \quad \Delta V = -\int_i^f \vec{E} \cdot d\vec{s}$$

$$U = k \frac{q_1 q_2}{r_{12}} \quad V = k \frac{q}{r} \quad \Delta U = q\Delta V \quad E_x = -\frac{\partial V}{\partial x}$$

$$\vec{p} = q\vec{d} \text{ (from - to +)} \quad \vec{\tau} = \vec{p} \times \vec{E} \quad U_{\text{dipole}} = -\vec{p} \cdot \vec{E}$$

$$\Phi_E = \int_S \vec{E} \cdot d\vec{A} \quad \oint_S \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_0} \quad \lambda \equiv \frac{\text{charge}}{\text{length}} \quad \sigma \equiv \frac{\text{charge}}{\text{area}} \quad \rho \equiv \frac{\text{charge}}{\text{volume}}$$

**Circuits:**

$$C = \frac{Q}{V} \quad \frac{1}{C_T} = \sum \frac{1}{C_i} \quad C_T = \sum C_i \quad C_0 = \frac{\epsilon_0 A}{d} \quad C = \kappa C_0$$

$$U = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C} = \frac{1}{2}QV \quad I = \frac{dq}{dt} \quad J = \frac{I}{A} \quad \vec{J} = nq\vec{v}_d$$

$$\vec{J} = \sigma\vec{E} \quad V = IR \quad R = \rho \frac{L}{A} \quad \sigma = \frac{1}{\rho} \quad \rho = \rho_0[1 + \alpha(T - T_0)]$$

$$\sum I = 0 \quad \sum \Delta V = 0 \quad \frac{1}{R_T} = \sum \frac{1}{R_i} \quad R_T = \sum R_i \quad P = IV = \frac{V^2}{R} = I^2 R$$

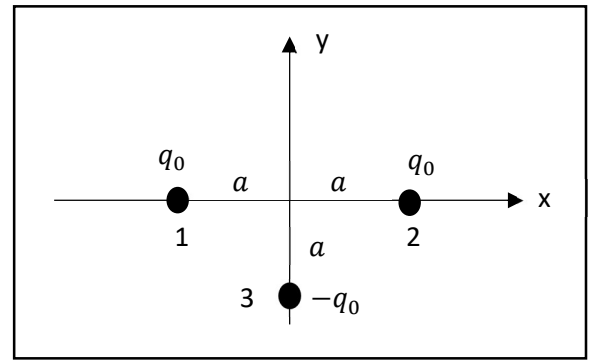
$$Q(t) = Q_{\text{final}}[1 - e^{-t/\tau}] \quad Q(t) = Q_0 e^{-t/\tau} \quad \tau = RC$$

**Integral:**

$$\int \frac{du}{(u^2 + a^2)^{3/2}} = \frac{u}{a^2 \sqrt{u^2 + a^2}} + c$$



6. Three point charges are arranged as illustrated where  $q_0 > 0$ . Point charge 1, with charge  $q_0$ , is placed at  $(-a, 0)$ . Another point charge 2 is placed at  $(a, 0)$  with the same charge  $q_0$ . A final charge 3 with a negative charge  $-q_0$  is placed at  $(0, -a)$ .



- (10) a. Compute the electrical Coulomb force charge 1 exerts on charge 2.

$$\vec{F}_{12} =$$

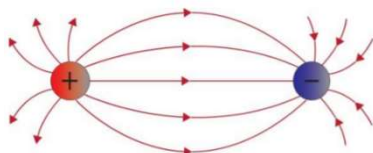
- (10) b. Compute the electric field at the origin due to the three charges.

$$\vec{E} =$$

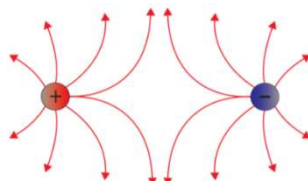
- (10) c. If a fourth charge  $q_4$  were placed at the origin, determine the electrical force it would experience from the three charges.

$$\vec{F} =$$

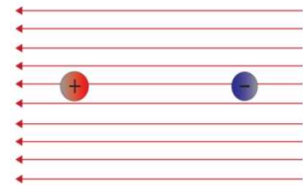
- (10) d. Which of the following represents the electric field due to one positive and one negative charge? Circle your answer.



A

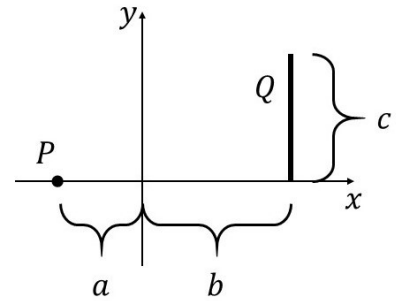


B



C

7. A positive charge  $Q$  is uniformly distributed along a line from  $(b, 0)$  to  $(b, c)$  as illustrated. The point  $P$  is located at  $(-a, 0)$ .



- (25) a. Write an integral to determine the electric potential at  $P$  due to the line of charge. [Do not solve the integral.]

$$V =$$

- (10) b. Let  $V_0$  be the value of the integral from part a. A particle of mass  $m_0$  and positive charge  $q_0$  is released from rest at point  $P$ . Determine the final speed of the particle.

$$v =$$

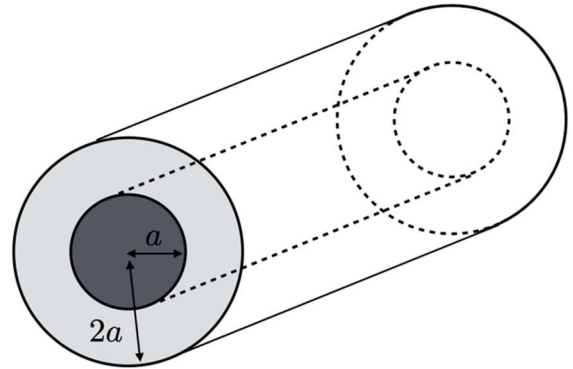
- (5) c. The potential in a given region of space is  $V = 3xyz^2$  (V/m<sup>4</sup>). Determine the  $z$ -component of the electric field in the region.

$$E_z =$$

$$/40$$

8. An infinitely long cable has an **insulating** cylinder with radius  $a$  with uniform charge volume density  $2\rho$  surrounded by a uniform **conducting** material with outer radius of  $2a$  and zero total charge, as shown.

- (15) a. Using Gauss's law, find the electric field **inside** the insulating cylinder. Draw a Gaussian surface and indicate your choice of a coordinate system.



$$\vec{E} =$$

- (10) b. Find the inner and outer charge surface density of the conducting cylinder,  $\sigma_{in}$  and  $\sigma_{out}$ .

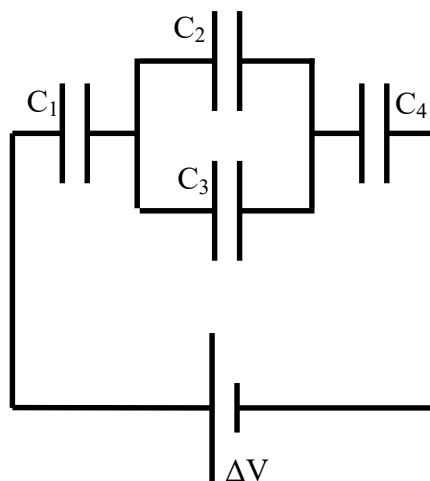
$$\sigma_{in} =$$

$$\sigma_{out} =$$

- (15) c. Determine the work required to move a charge  $q_0$  from  $r_i = 4a$  to  $r_f = 1.57a$  where  $r$  is the distance from the cylindrical axis.

$$W =$$

9. For the capacitor circuit shown  $C_1 = 3 \mu\text{F}$ ,  $C_2 = 4 \mu\text{F}$ ,  $C_3 = 2 \mu\text{F}$ , and  $C_4 = 2 \mu\text{F}$ .  
 (10) a. Find the equivalent capacitance.



$C_E =$
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- (30) b. The charge on capacitor  $C_1$  is  $3 \mu\text{C}$ . Determine the charge on the other capacitors, and the applied voltage  $\Delta V$ .

$Q_2 =$
$Q_3 =$
$Q_4 =$
$\Delta V =$