## Official Starting Equations

## PHYS 2135, Engineering Physics II

From PHYS 1135:
$x=x_{0}+v_{0 x} \Delta t+\frac{1}{2} a_{x}(\Delta t)^{2} \quad v_{x}=v_{0 x}+a_{x} \Delta t \quad v_{x}^{2}=v_{0 x}^{2}+2 a_{x}\left(x-x_{0}\right) \quad \sum \vec{F}=m \vec{a}$
$F_{r}=-\frac{m v_{t}^{2}}{r} \quad P=\frac{F}{A} \quad \vec{p}=m \vec{v} \quad P=\frac{d W}{d t} \quad W=\int \vec{F} \cdot d \vec{s}$
$K=\frac{1}{2} m v^{2} \quad U_{f}-U_{i}=-W_{\text {conservative }} \quad E=K+U \quad E_{f}-E_{i}=\left(W_{\text {other }}\right)_{i \rightarrow f} \quad E=P_{\text {ave }} t$

## Constants:

$g=9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}} \quad m_{\text {electron }}=9.11 \times 10^{-31} \mathrm{~kg}$
$m_{\text {proton }}=1.67 \times 10^{-27} \mathrm{~kg}$
$e=1.6 \times 10^{-19} \mathrm{C}$
$c=3.0 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}} \quad k=\frac{1}{4 \pi \epsilon_{0}}=9 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}} \quad \epsilon_{0}=8.85 \times 10^{-12} \frac{\mathrm{C}^{2}}{\mathrm{Nm}^{2}} \quad \mu_{0}=4 \pi \times 10^{-7} \frac{\mathrm{Tm}}{\mathrm{A}}$

## Electric Force, Field, Potential and Potential Energy:

$\vec{F}=k \frac{q_{1} q_{2}}{r_{12}^{2}} \hat{r}_{12}$
$\vec{E}=k \frac{q}{r^{2}} \hat{r}$
$\vec{F}=q \vec{E}$
$\Delta V=-\int_{i}^{f} \vec{E} \cdot d \vec{s}$
$U=k \frac{q_{1} q_{2}}{r_{12}}$
$V=k \frac{q}{r}$
$\Delta U=q \Delta V$
$E_{x}=-\frac{\partial V}{\partial x}$
$\vec{p}=q \vec{d}($ from - to +$)$
$\vec{\tau}=\vec{p} \times \vec{E}$
$U_{\text {dipole }}=-\vec{p} \cdot \vec{E}$
$\Phi_{E}=\int_{S} \vec{E} \cdot d \vec{A}$
$\oint_{S} \vec{E} \cdot d \vec{A}=\frac{q_{\text {enclosed }}}{\epsilon_{0}}$
$\lambda \equiv \frac{\text { charge }}{\text { length }}$
$\sigma \equiv \frac{\text { charge }}{\text { area }} \quad \rho \equiv \frac{\text { charge }}{\text { volume }}$

## Circuits:

$C=\frac{Q}{V} \quad \frac{1}{c_{T}}=\sum \frac{1}{c_{i}}$
$C_{T}=\sum C_{i}$
$C_{0}=\frac{\epsilon_{0} A}{d}$
$C=\kappa C_{0}$
$U=\frac{1}{2} C V^{2}=\frac{1}{2} \frac{Q^{2}}{C}=\frac{1}{2} Q V$
$I=\frac{d q}{d t}$
$J=\frac{I}{A}$
$\vec{J}=n q \vec{v}_{d}$
$\vec{J}=\sigma \vec{E} \quad V=I R$
$R=\rho \frac{L}{A}$
$\sigma=\frac{1}{\rho}$
$\rho=\rho_{0}\left[1+\alpha\left(T-T_{0}\right)\right]$
$\sum I=0$
$\sum \Delta V=0$
$Q(t)=Q_{\text {final }}\left[1-e^{-t / \tau}\right]$
$\frac{1}{R_{T}}=\sum \frac{1}{R_{i}}$
$R_{T}=\sum R_{i}$
$P=I V=\frac{V^{2}}{R}=I^{2} R$
$Q(t)=Q_{0} e^{-t / \tau} \quad \tau=R C$

## Integral:

$\int \frac{d u}{\left(u^{2}+a^{2}\right)^{3 / 2}}=\frac{u}{a^{2} \sqrt{u^{2}+a^{2}}}+c$

## Exam Total

## PHYS 2135 Exam I

February 15, 2022
Name: $\qquad$ Section: $\qquad$

For questions $1-5$, select the best answer. For problems $6-9$, solutions must begin with an Official Starting Equation, when appropriate. Work must be shown to receive credit. Calculators are not allowed. Use appropriate units. Provide answers in terms of given variable and fundamental constants.
(8) $\qquad$ 1. A negatively charge particle is released from rest between two equipotentials. The particle will ...
[A] accelerate toward the region of higher potential.
[B] accelerate toward the region of lower potential.
[C] accelerate parallel to the equipotentials.
[D] remain at rest.

(8) $\qquad$ 2. A dipole is initially spinning clockwise in a uniform electric field. At the moment illustrated, the angular speed is ...
[A] decreasing.
[B] remaining constant.
[C] increasing.

(8) $\qquad$ 3. A parallel plate capacitor with capacitance $C_{0}$ and gap distance $d_{0}$ is charged using a battery with potential $V_{B}$. After the capacitor is fully charged, the battery is disconnected and then the gap distance is changed to $\frac{1}{4} d_{0}$. Determine the final potential across the capacitor.
[A] $\quad V_{f}=0$
[B] $\quad V_{f}=\frac{1}{4} V_{B}$
[C] $\quad V_{f}=V_{B}$
[D] $\quad V_{f}=4 V_{B}$
(8) $\qquad$ 4. The dashed boundary represents a gaussian surface in the presence of two charges, . Determine the total flux through the gaussian surface.

[A] $\quad-\frac{2 q_{0}}{\epsilon_{0}}$
[B] $-\frac{q_{0}}{\epsilon_{0}}$
[C] $+\frac{q_{0}}{\epsilon_{0}}$
[D] $\quad+\frac{2 q_{0}}{\epsilon_{0}}$
(8) $\qquad$ 5. (Free) The recent snowstorm was unfortunate because.
[A] Reduced friction should be limited to physics $I$.
[B] The snow hides the fields.
[C] Energy is not conserved when walking through drifts.
[D] Vehicles were static.
6. Three point charges are arranged as illustrated where $q_{0}>0$. Point charge 1 , with charge $q_{0}$, is placed at ( $-\mathrm{a}, 0$ ). Another point charge 2 is placed at $(a, 0)$ with the same charge $q_{0}$. A final charge 3 with a negative charge $-q_{0}$ is placed at $(0,-a)$.

(10) a. Compute the electrical Coulomb force charge 1 exerts on charge 2.

$$
\vec{F}_{12}=
$$

(10) b. Compute the electric field at the origin due to the three charges.
$\vec{E}=$
(10) c. If a fourth charge $q_{4}$ were placed at the origin, determine the electrical force it would experience from the three charges.
$\qquad$
(10) d. Which of the following represents the electric field due to one positive and one negative charge? Circle your answer.

7. A positive charge $Q$ is uniformly distributed along a line from $(b, 0)$ to $(b, c)$ as illustrated. The point $P$ is located at $(-a, 0)$.

(25) a. Write an integral to determine the electric potential at $P$ due to the line of charge. [Do not solve the integral.]

$$
V=
$$

(10) b. Let $V_{0}$ be the value of the integral from part a. A particle of mass $m_{0}$ and positive charge $q_{0}$ is released from rest at point $P$. Determine the final speed of the particle.

$$
v=
$$

(5) c. The potential in a given region of space is $V=3 x y z^{2}\left(\mathrm{~V} / \mathrm{m}^{4}\right)$. Determine the $z$-component of the electric field in the region.

8. An infinitely long cable has an insulating cylinder with radius $a$ with uniform charge volume density $2 \rho$ surrounded by a uniform conducting material with outer radius of $2 a$ and zero total charge, as shown.
(15)
a. Using Gauss's law, find the electric field inside the insulating cylinder. Draw a Gaussian surface and indicate your choice of a coordinate system.


$$
\vec{E}=
$$

(10) b. Find the inner and outer charge surface density of the conducting cylinder, $\sigma_{\text {in }}$ and $\sigma_{\text {out }}$.

$$
\begin{gathered}
\sigma_{\text {in }}= \\
\\
\sigma_{\text {out }}=
\end{gathered}
$$

(15) c. Determine the work required to move a charge $q_{0}$ from $r_{i}=4 a$ to $r_{f}=1.57 a$ where $r$ is the distance from the cylindrical axis.

9. For the capacitor circuit shown $C_{1}=3 \mu \mathrm{~F}, \mathrm{C}_{2}=4 \mu \mathrm{~F}, \mathrm{C}_{3}=2 \mu \mathrm{~F}$, and $\mathrm{C}_{4}=2 \mu \mathrm{~F}$.
(10) a. Find the equivalent capacitance.


$$
C_{E}=
$$

(30) b. The charge on capacitor $C_{1}$ is $3 \mu \mathrm{C}$. Determine the charge on the other capacitors, and the applied voltage $\Delta \mathrm{V}$.

| $Q_{2}=$ |
| :--- |
| $Q_{3}=$ |
| $Q_{4}=$ |
| $\Delta V=$ |



