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PHYS 2135 Exam I
September 18, 2018

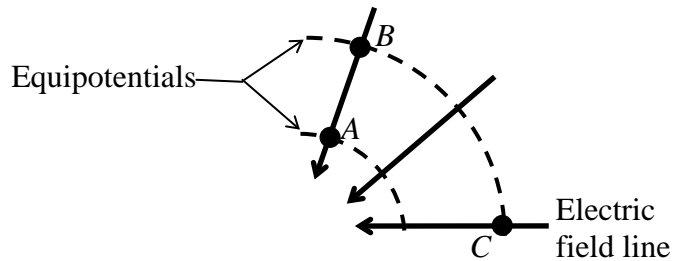
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For questions 1-5, select the best answer. For problems 6-9, solutions must begin with an Official Starting Equation, when appropriate. Work must be shown to receive credit. Calculators are not allowed.

- (8) **C** 1. A Gaussian sphere of radius R is centered on a positive charge Q . If the radius of the sphere is doubled the net electric flux through the Gaussian surface is ...
- [A] doubled
 - [B] halved
 - [C] unchanged
 - [D] reduced by a factor of four

- (8) **B** 2. You are given three charged insulating spheres. Spheres 1 and 2 are found to attract each other. Spheres 2 and 3 are found to repel each other. Which of the following can you conclude?
- [A] Spheres 1 and 3 carry charges of equal sign
 - [B] Spheres 1 and 3 carry charges of opposite sign
 - [C] All three spheres carry charges of the same sign
 - [D] Spheres 1 and 3 will repel each other

- (8) **B** 3. The figure shows the electric field lines and equipotentials in a certain region of space. Which of the following is true?
- [A] $V_A > V_B$ and $V_B = V_C$
 - [B] $V_B > V_A$ and $V_B = V_C$
 - [C] $V_C > V_B$ and $V_A = V_B$
 - [D] $V_A = V_B = V_C$



- (8) **B** 4. The capacitance of a parallel-plate capacitor can be increased ...
- [A] by increasing charge on each plate.
 - [B] by increasing the area of each plate.
 - [C] by increasing spacing between the plates.
 - [D] by increasing the potential difference across the plates.

- (8) _____ 5. What do the San Diego Chargers have in common with PHYS 2135 students?
- | | |
|--------------------------|-----------------|
| [A] Great Potential | [B] Field Lines |
| [C] Formulas for Success | [D] More Points |

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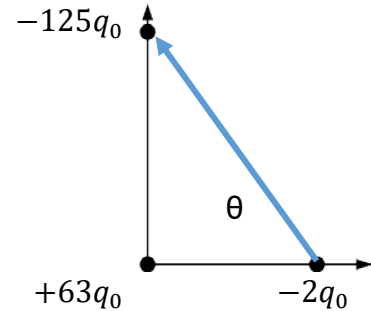
6. There is a positive charge $+63q_0$ at the origin and a negative charge $-125q_0$ located at $(x,y) = (0, 4a)$. Start with an OSE and express your answers in terms of k, q_0, m and the given quantities. For vectors, express your answers in unit vector notation.

- (15) (a) What is the electric field at $(x,y) = (3a, 0)$ due to the $+63q_0$ charge?

$$\vec{E} = k \frac{q}{r^2} \hat{r}$$

$$\vec{E}_{63} = \frac{k(63q_0)}{(3a)^2} \hat{i}$$

$$\vec{E}_{63} = \frac{7kq_0}{a^2} \hat{i}$$



- (15) (b) What is the electric field at $(x,y) = (3a, 0)$ due to the $-125q_0$ charge?

$$\vec{E}_{125} = \frac{k(-125q_0)}{(5a)^2} [\cos \theta \hat{i} - \sin \theta \hat{j}]$$

$$\sin \theta = \frac{4}{5} \quad \cos \theta = \frac{3}{5}$$

$$\vec{E}_{125} = \frac{5kq_0}{a^2} \left[-\frac{3}{5} \hat{i} + \frac{4}{5} \hat{j} \right]$$

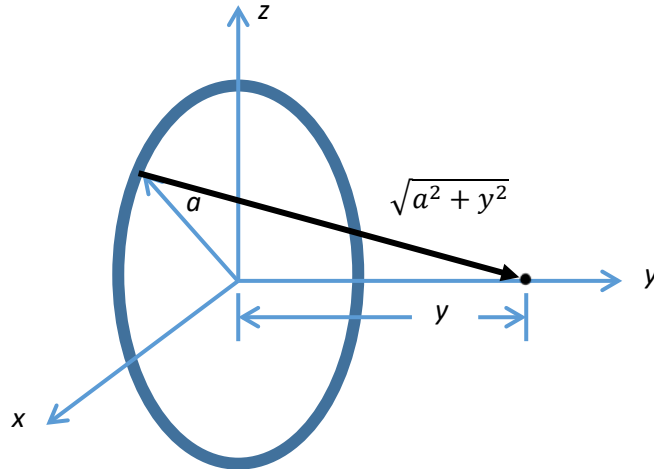
$$\vec{E}_{125} = \frac{kq_0}{a^2} [-3\hat{i} + 4\hat{j}]$$

- (5) (c) A particle with a negative charge $-2q_0$ and mass m is placed at $(3a, 0)$. What is the net force on this particle?

$$\vec{E}_{Tot} = \vec{E}_{63} + \vec{E}_{125} = \frac{kq_0}{a^2} [4\hat{i} + 4\hat{j}]$$

$$\vec{F} = (-2q_0)\vec{E}_{Tot} = \frac{-8kq_0^2}{a^2} [\hat{i} + \hat{j}]$$

7. An insulating ring of radius a has a net charge $+Q$ uniformly distributed along the ring. The ring lies in the x - z plane with the origin of the coordinate system at the center of the ring. The y -axis is perpendicular to the ring and is on a line through the center of the ring.



- (10) (a) Determine the linear charge density λ on the ring.

$$\lambda = \frac{Q}{2\pi a}$$

- (15) (b) Set up and evaluate an integral to determine the electric potential as a function of y along the y -axis.

$$V = k \int_0^{2\pi} \frac{dq}{\sqrt{a^2 + y^2}} \quad dq = \lambda a d\theta$$

$$V = k \int_0^{2\pi} \frac{\lambda a d\theta}{\sqrt{a^2 + y^2}} = \frac{k\lambda a}{\sqrt{a^2 + y^2}} \int_0^{2\pi} d\theta = \frac{2\pi k\lambda a}{\sqrt{a^2 + y^2}}$$

$$V = \frac{kQ}{\sqrt{a^2 + y^2}}$$

- (15) (c) A particle of mass m and charge $-q_0$ is placed at $y = 2a$ and released from rest. Determine the speed of the particle as it passes through the center of the ring.

$$E_f - E_i = W_{other} = 0$$

$$U = qV = -q_0V$$

$$U_f + K_f = U_i + K_i$$

$$U_f = -\frac{kq_0Q}{a}$$

$$U_i = -\frac{kq_0Q}{a\sqrt{5}}$$

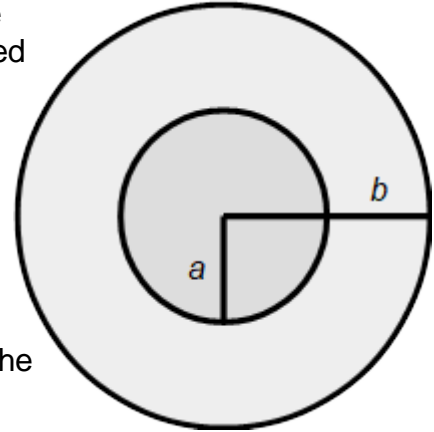
$$-\frac{kq_0Q}{a} + \frac{1}{2}mv_f^2 = -\frac{kq_0Q}{a\sqrt{5}}$$

$$v_f = \sqrt{\frac{2}{m} \left(\frac{kq_0Q}{a} \right) \left[1 - \frac{1}{\sqrt{5}} \right]}$$

8. A solid **insulating** plastic sphere of radius a carries a total net negative charge $-Q$ uniformly distributed throughout its interior. The insulating sphere is coated with a **conducting** metallic layer in the form of a spherical shell with inner radius a and outer radius b . The conducting layer carries a net charge of $+Q$.

- (5) (a) Compute the volume charge density ρ in the plastic sphere in terms of variables introduced above.

$$\rho = \frac{q}{V} = \frac{-Q}{\frac{4}{3}\pi a^3} = \frac{-3Q}{4\pi a^3}$$



- (10) (b) Apply Gauss's law to find the magnitude of the electric field $E(r)$ in the region $r < a$.

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0} \quad q_{enc} = \rho \left(\frac{4}{3}\pi r^3 \right) \quad \text{or} \quad q_{enc} = -Q \left(\frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi a^3} \right) = -Q \left(\frac{r^3}{a^3} \right)$$

$$E(4\pi r^2) = \frac{\rho \left(\frac{4}{3}\pi r^3 \right)}{\epsilon_0} \quad \text{or} \quad E(4\pi r^2) = \frac{-Q \left(\frac{r^3}{a^3} \right)}{\epsilon_0}$$

$$E = \frac{\rho r}{3\epsilon_0} \quad \text{or} \quad |E| = \frac{Qr}{4\pi\epsilon_0 a^3}$$

- (10) (c) Find the electric field at points in the region $b > r > a$. Justify your answer.

$$E = 0 \quad \text{The electric field is zero inside the conductor.}$$

- (10) (d) Find the charge density on the inner surface of the spherical shell.

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0} = 0$$

$$q_{enc} = 0 = -Q + Q_a$$

$$Q_a = Q$$

$$\sigma_a = \frac{Q_a}{4\pi a^2} = \frac{Q}{4\pi a^2}$$

- (5) (e) Find the electric field at points in the region $r > b$.

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0} = \frac{-Q+Q}{\epsilon_0} = 0$$

$$E = 0$$

9. Consider the given circuit.

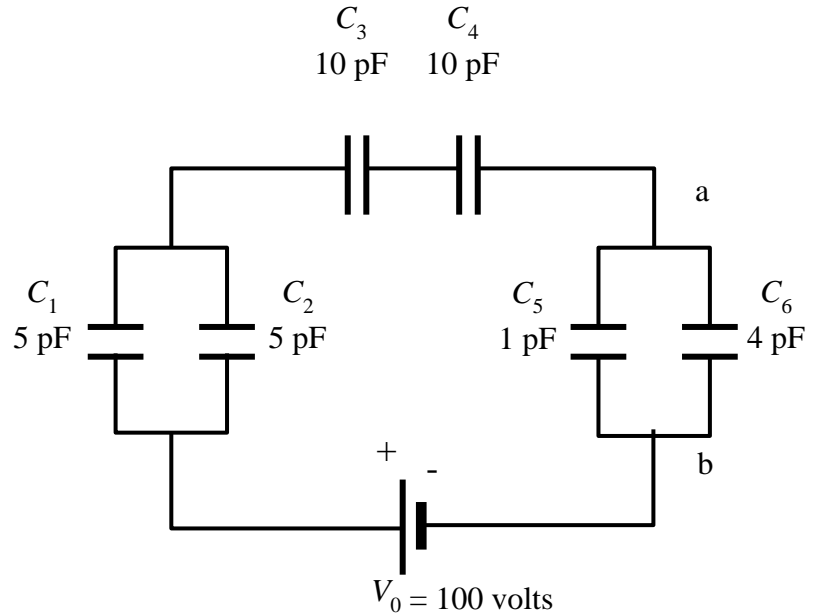
- (10) (a) Calculate the equivalent capacitance of the entire circuit.
(Note: $1 \text{ pF} = 10^{-12} \text{ F}$)

$$C_{12} = 5 \text{ pF} + 5 \text{ pF} = 10 \text{ pF}$$

$$C_{56} = 1 \text{ pF} + 4 \text{ pF} = 5 \text{ pF}$$

$$C_{eq} = \left(\frac{1}{10 \text{ pF}} + \frac{1}{10 \text{ pF}} + \frac{1}{10 \text{ pF}} + \frac{1}{5 \text{ pF}} \right)^{-1}$$

$$C_{eq} = 2 \text{ pF}$$



- (10) (b) Find the charge Q_3 on capacitor C_3 .

$$Q_3 = Q_{eq} = C_{eq} V_0 = (2 \text{ pF})(100 \text{ V}) = 200 \text{ pC}$$

- (10) (c) Find the voltage V_1 across capacitor C_1 .

$$V_{12} = \frac{Q_{12}}{C_{12}} = \frac{Q_{eq}}{C_{12}} = \frac{200 \text{ pC}}{10 \text{ pF}} = 20 \text{ V}$$

- (10) (d) Capacitor C_5 is a parallel plate capacitor, with the dimensions indicated. Determine the spacing d between the plates of this capacitor (a numerical answer is required.)

$$C_5 = \frac{\epsilon_0 A}{d} = \frac{\epsilon_0 L^2}{d}$$

$$d = \frac{\epsilon_0 L^2}{C_5} = \frac{(8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2})(10^{-2} \text{ m})^2}{10^{-12} \text{ F}}$$

$$d = 8.85 \times 10^{-4} \text{ m}$$

