1. (40 points total) Three positively charged spheres lie at the corners of a rectangle of sides $8L$ and $15L$, as shown in the diagram. Start with OSEs and express all answers in unit vector notation.

(a) (10 points) Find the electric field vector due to $Q_1$ at the location of $Q_3$. 

(b) (20 points) Find the electric field vector due to $Q_2$ at the location of $Q_3$. 

(c) (10 points) If all other charges are held stationary, what is the net force exerted on $Q_3$ at the instant shown?
2. (20 points total) A simple circuit. All solutions MUST start with OSE’s.

(a) (10 points) Two lamps of resistance $R_1$ and $R_2$ are connected to a 12 V battery as shown. The lamps draw 24 W and 48 W of power, respectively. Find $R_1$ and $R_2$.

(b) (10 points) A 12 volt battery is connected to three resistors as shown. What is the equivalent resistance of the entire circuit? What is the current through the 7 Ω resistor?

3. (20 points total) Motional emf. All solutions MUST start with OSE’s.

(a) (10 points) A stationary conducting loop is placed in the xy-plane in a uniform magnetic field. Circle any of the following that have current induced in the loop.

(b) (10 points) A different conducting loop of constant radius $R$ is in a region of uniform magnetic field $\vec{B}$ in the $-z$ direction. The loop is rotated at a constant angular speed $\omega$ about an axis in the xy plane, passing through the center of the loop and in $+y$ direction as shown. Derive an expression for the emf induced in the loop.
4. (20 points total) A chlorine ion of charge \(-e\) and mass \(m = 5.81 \times 10^{-26}\) kg is moving with speed \(v = 2 \times 10^5\) m/s under the influence of both a magnetic field and an electric field. Both fields are perpendicular to each other and to the ion’s velocity. The magnitude of the magnetic field is \(B = 3 \times 10^{-3}\) T.

(a) (5 points) You observe that the ion moves straight ahead without being deflected. What is the direction of the electric field? (circle one of the symbols below)

\[ \uparrow \quad \downarrow \quad \rightarrow \quad \leftarrow \quad \otimes \quad \bigcirc \]

(b) (5 points) Find the magnitude of the electric field.

(c) (10 points) The electric field is now switched off, and the ion moves in a circular orbit. Find the period of this orbit.

5. (20 points total) A square wire loop of side \(L\) carries a current \(I\). It is in a uniform magnetic field \(\vec{B}\) pointing upwards. The loop is tilted \(45^\circ\) with respect to the horizontal as shown in the figure.

(a) (5 points) Find the net force on the loop.

(b) (10 points) Find the magnitude of the torque on the loop.

(c) (5 points) In the side view above, what is the direction of the torque vector \(\vec{\tau}\)? (circle one of the symbols below)

\[ \uparrow \quad \downarrow \quad \rightarrow \quad \leftarrow \quad \otimes \quad \bigcirc \]
6. (30 points total) A 10 mm tall object is placed 15 cm to the left of a thin diverging lens that has a focal length of magnitude 10 cm.

(a) (10 points) Find the image position.

(b) (10 points) Calculate the image height.

(c) (10 points) Complete a ray diagram showing the formation of the image using the figure provided below. Adjacent marks on the principal axis are separated by 5.0 cm. You need show only two rays.

7. (10 points total) An object is placed 6 cm to the left of a thin converging lens that has a focal length of magnitude 24 cm. The image is formed 8 cm from the lens, on the same side of the lens as the object.

(a) (5 points) Is the image REAL or VIRTUAL (circle one)?

(b) (5 points) Is the image UPRIGHT or INVERTED (circle one)?
8. (20 points total) A ray of light traveling in a block of glass ($n_g = 1.56$) is incident on the bottom surface at an angle of $60^\circ$ with respect to the normal.

(a) (15 points) If a film is placed on the bottom surface of the glass, the ray is totally reflected. What is the maximum possible index of refraction of the film?

(b) (5 points) Which of the two rays in the figure to the right will pass through the film? (circle one below)

RAY A  RAY B

9. (20 points total) A pair of eye glasses ($n_g = 1.5$) are coated with a film on the inner side of the lens (the side of the lens closest to the eye) to reduce reflection from 560 nm light which comes from behind the person. If the index of refraction of the film is 1.4, what is the minimum thickness of the film?